EScala3 enum for a te Monad Algebraic Da

- **Explore a terser definition of the Option Monad that uses a Scala 3 enumate.**
- In the process, have a tiny bit of fun with **Scala 3 enums**.
- Get a refresher on the **Functor** and **Monad** laws.
- See how easy it is to use **Scala 3 extension** methods, e.g. to add conven

We introduce a new type, **Option**. As we mentioned earlier, this type also exists in the **Option** is mandatory! Do not use **null** to denote that an optional value is absent. Let's have a **Scala** standard library, but we're re-creating it here for pedagogical purposes: look at how **Option** is defined: **sealed abstract class Option**[**+A**] **extends IterableOnce**[**A**] **sealed trait Option**[+A] **final case class Some**[**+A**](value: A) **extends Option**[**A**] **case class Some**[+A](get: A) **extends Option**[A] **case object None extends Option**[**Nothing**] **case object None extends Option**[**Nothing**] Jejandro Serras Over the years we have all got very used to Functional **BOOK** the definition of the **Option monad**'s Programming for Mortals **Algebraic Data Type** (**ADT**).OF MONADS **Scala from** with Scalaz Scratch Sam Halliday Gfommil er the theory and peactice of n
applied to solve real world pr Since creating new data types is so cheap, and it is possible to work with them We have already encountered **scalaz**'s improvement over scala.Option, called **Maybe**. It is polymorphically, most functional languages define some notion of an **optional value**. In an improvement because it does not have any unsafe methods like **Option.get**, which can **Haskell** it is called **Maybe**, in **Scala** it is **Option**, … Regardless of the language, the throw an exception, and is invariant. structure of the data type is similar: It is typically used to represent when a thing may be present or not without giving any extra **data Maybe** a = **Nothing** –- no value context as to why it may be missing. | **Just** a -- holds a value **sealed abstract class Maybe**[A] { ... } **sealed abstract class** Option[**+A**] // optional value **object Maybe** { **case object** None **extends** Option[**Nothing**] // no value **final case class Empty**[A]() **extends Maybe**[A] **case class** Some[**A**](value: **A**) **extends** Option[**A**] // holds a value **final case class Just**[A](a: A) **extends Maybe**[A]

With the arrival of **Scala 3** however, the definition of the **Option ADT** becomes much terser thanks to the fact that it can be implemented using the new **enum** concept .

Scala 3/Reference/Enums/Algebraic Data Types

Algebraic Data Types

2 Edit this page on GitHub

The enum concept is general enough to also support algebraic data types (ADTs) and their generalized version (GADTs). Here is an example how an Option type can be represented as an ADT:

enum $Option[+T]$ { case Some $(x: T)$ case None

Martin Odersky *<u> @odersky</u>*

OK, so this is, again, cool, **now we have parity with Java**, **but we can actually go way further**. **enums can not only have value parameters, they also can have type parameters, like this**.

#1 Enums

can have type parameters, making them algebraic data types (ADTs)

You Tube A Tour of Scala $3 - by$ Martin Odersky

So you can have an **enum Option** with a **covariant** type parameter **T** and then two cases **Some** and **None**.

So that of course gives you what people call an Algebraic Data Type, or ADT.

Scala so far was lacking a simple way to write an ADT. What you had to do is essentially what the compiler would translate this to.

Martin Odersky @odersky

So the compiler would take this **ADT** that you have seen here and translate it into essentially this:

#1 Enums sealed abstract class Option[+T] object Option { case class Some[+T](x: T) extends Option[T] object Some { def apply $[T](x: T)$: Option $[T] = Some(x)$ val None = new Option [Nothing] $\{ \ldots \}$

compile to sealed hierarchies of case classes and objects.

You Tube A Tour of Scala $3 - by$ Martin Odersky

And so far, if you wanted something like that, you would have written essentially the same thing. So **a sealed** abstract class or a sealed abstract trait, Option, with a case class as one case, and as the other case, here it is **a val, but otherwise you could also use a case object**.

And that of course is completely workable, but it is kind of tedious. When Scala started, one of the main **motivations, was to avoid pointless boilerplate**. So that's why **case classes** were invented, and **a lot of other innovations that just made code more pleasant to write and more compact than Java code**, the standard at the time.

On the next slide we have a go at adding some essential methods to this terser **enum**-based **Option ADT**.

enum Option[+A**]**: **case Some(**a: A**) case None**

@philip_schwarz

Option is a **monad**, so we have given it a **flatMap** method and a **pure** method. In **Scala** the latter is not strictly needed, but we'll make use of it later.

Every **monad** is also a **functor**, and this is reflected in the fact that we have given **Option** a **map** method.

We gave **Option** a **fold** method, to allow us to **interpret/execute** the **Option effect**, i.e. to escape from the **Option** container, or as **John a De Goes** puts it, to **translate away** from **optionality** by providing a **default value**.

We want our **Option** to integrate with **for comprehensions** sufficiently well for our current purposes, so in addition to **map** and **flatMap** methods, we have given it a simplistic **withFilter** method that is just implemented in terms of **filter**, another pretty essential method.

There are of course many many other methods that we would normally want to add to **Option**.

```
enum Option[+A]:
  case Some(a: A)
  case None
  def map[B](f: A => B): Option[B] =
    this match
      case Some(a) => Some(f(a))
      case None => None
  def flatMap[B](f: A => Option[B]): Option[B] =
    this match
      case Some(a) \Rightarrow f(a)case None => None
  def fold[B](ifEmpty: => B)(f: A => B) =
    this match
      case Some(a) \Rightarrow f(a)case None => ifEmpty
  def filter(p: A => Boolean): Option[A] =
    this match
      case Some(a) if p(a) \Rightarrow Some(a)
      case _ => None
  def withFilter(p: A => Boolean): Option[A] =
    filter(p)
object Option : 
  def pure[A](a: A): Option[A] = Some(a)
```

```
def none: Option[Nothing] = None
extension[A](a: A):
```
def some: **Option[**A**]** = **Some(**a**)**

The **some** and **none** methods are just there to provide the convenience of **Cats**-like syntax for **lifting** a **pure** value into an **Option** and for referring to the **empty Option** instance.

Yes, the **some** method on the previous slide was implemented using the new **Scala 3** feature of **Extension Methods**.

Scala 3/Reference/Contextual Abstractions/Extension Methods

Extension Methods

2 Edit this page on GitHub

Extension methods allow one to add methods to a type after the type is defined. Example:

case class Circle(x: Double, y: Double, radius: Double)

extension (c: Circle) def circumference: Double = c.radius * math.Pi * 2

Like regular methods, extension methods can be invoked with $\ln x$.

val circle = $Circle(0, 0, 1)$ circle.circumference

On the next slide we do the following:

- See our **Option monad ADT** again
- Define a few **enumerated types** using use the **Scala 3 enum** feature.
- Add a simple program showing the **Option monad** in action.

```
enum Option[+A]:
  case Some(a: A)
  case None
  def map[B](f: A => B): Option[B] =
   this match
      case Some(a) => Some(f(a))
      case None => None
  def flatMap[B](f: A => Option[B]): Option[B] =
   this match
     case Some(a) => f(a)
      case None => None
  def fold[B](zero: => B)(f: A => B) =
    this match
      case Some(a) => f(a)
      case None => zero
  def filter(p: A => Boolean): Option[A] =
    this match
     case Some(a) if p(a) = > Some(a)
     case _ => None
  def withFilter(p: A => Boolean): Option[A] =
   filter(p)
object Option : 
  def pure[A](a: A): Option[A] = Some(a)
  def none: Option[Nothing] = None
extension[A](a: A):
 def some: Option[A] = Some(a)
                                                       enum Greeting(val language: Language):
                                                         override def toString: String = 
                                                           s"${enumLabel} ${language.toPreposition}"
                                                         case Welcome extends Greeting(English)
                                                         case Willkommen extends Greeting(German)
                                                         case Bienvenue extends Greeting(French)
                                                         case Bienvenido extends Greeting(Spanish)
                                                         case Benvenuto extends Greeting(Italian) 
                                                                                                        enum Language(val toPreposition: String):
                                                                                                          case English extends Language("to")
                                                                                                          case German extends Language("nach")
                                                                                                          case French extends Language("à")
                                                                                                          case Spanish extends Language("a") 
                                                                                                          case Italian extends Language("a")
                                                       enum Planet:
                                                         case Mercury, Venus, Earth, Mars, Jupiter, Saturn, Neptune, Uranus, Pluto, Scala3
                                                       case class Earthling(name: String, surname: String, languages: Language*) 
                                                       def greet(maybeGreeting: Option[Greeting], 
                                                                 maybeEarthling: Option[Earthling], 
                                                                 maybePlanet: Option[Planet]): Option[String] = 
                                                         for
                                                           greeting <- maybeGreeting 
                                                           earthling <- maybeEarthling
                                                           planet <- maybePlanet
                                                           if earthling.languages contains greeting.language
                                                         yield s"$greeting $planet ${earthling.name}!"
                                                       @main def main =
                                                         val maybeGreeting = 
                                                           greet( maybeGreeting = Some(Welcome),
                                                                  maybeEarthling = Some(Earthling("Fred", "Smith", English, Italian)),
                                                                     maybePlanet = Some(Scala3))
                                                         println(maybeGreeting.fold("Error: no greeting message")
```

```
(msg => s"*** $msg ***"))
```
*** Welcome to Scala3 Fred! ***

Same again, but this time using the **some** and **none** convenience methods.

The remaining slides provide us with a refresher of the **functor** and **monad laws**. To do so, they use two examples of ordinary functions and three examples of **Kleisli arrows**, i.e. functions whose signature is of the form A => F[B], for some **monad** F, which in our case is the **Option monad**.

The example functions are defined below, together with a function that uses them. While the functions are bit contrived, they do the job.

The reason why the **Kleisli arrows** are a bit more complex than would normally be expected is that since in this slide deck we are defining our own simple **Option monad**, we are not taking shortcuts that involve the standard **Scala Option**, e.g. converting a **String** to an **Int** using the **toIntOption** function available on **String**.

val double: Int => Int = $n =$ \geq \geq \neq $n =$ **val square:** Int => Int = $n => n * n$

val stringToInt: String => **Option[**Int**]** = s => Try **{** s.toInt **}**.fold**(**_ => **None**, **Some(**_**))**

val intToChars: Int => **Option[**List**[**Char**]]** = n => **if** n < 0 **then None else Some(**n.toString.toArray.toList**)**

```
val charsToInt: Seq[Char] => Option[Int] = chars => 
 Try { 
    chars.foldLeft(0){ (n, char) => 10 * n + char.toString.tolnt }
 }.fold(_ => None, Some(_))
```
def doublePalindrome(s: String**)**: **Option[**String**]** = **for**

```
n <- stringToInt(s)
       chars <- intToChars(2 * n)
  palindrome <- charsToInt(chars ++ chars.reverse) 
yield palindrome.toString
```
assert**(stringToInt("123")** == **Some(**123**))** assert**(stringToInt("1x3")** == **None)**

assert**(intToChars(**123**)** == **Some(**List**('1'**, **'2'**, **'3')))** assert**(intToChars(**0**)** == **Some(**List**('0')))** assert**(intToChars(**-10**)** == **None)**

assert**(charsToInt(**List**('1'**, **'2'**, **'3'))** == **Some(**123**))** assert**(charsToInt(**List**('1'**, **'x'**, **'3'))** == **None)**

assert**(doublePalindrome("123")** == **Some("246642"))** assert**(doublePalindrome("1x3")** == **None)**

Since every **monad** is also a **functor**, the next slide is a reminder of the **functor** laws.

We also define a **Scala 3 extension method** to provide syntax for the infix operator for **function composition**.

```
// FUNCTOR LAWS
// identity law: ma map identity = identity(ma)
assert( (f(a) map identity) == identity(f(a)) )
assert( (a.some map identity) == identity(a.some) )
assert( (none map identity) == identity(none) ) 
// composition law: ma map (g ∘ h) == ma map h map g
assert( (f(a) map (g ∘ h)) == (f(a) map h map g) )
assert( (3.some map (g ∘ h)) == (3.some map h map g) )
assert( (none map (g ∘ h)) == (none map h map g) )
```


```
val f = stringToInt
  val g = double
  val h = square
  val a = "123"
  // plain function composition
  extension[A,B,C](f: B \Rightarrow C)def ∘ (g: A => B): A => C =
      a => f(g(a))
  def identity[A](x: A): A = x...
assert( stringToInt("123") == Some(123) )
assert( stringToInt("1x3") == None )
val double: Int => Int = n = \geq \geq \neq n =val square: Int => Int = n => n * n
```

```
enum Option[+A]:
 case Some(a: A)
 case None
 def map[B](f: A => B): Option[B] =
   this match
      case Some(a) => Some(f(a))
      case None => None
object Option : 
 def pure[A](a: A): Option[A] = Some(a)
 def none: Option[Nothing] = None
extension[A](a: A):
 def some: Option[A] = Some(a)
```


While the **functor Identity Law** is very simple, the fact that it can be formulated in slightly different ways can sometimes be a brief source of puzzlement when recalling the law.

On the next slide I have a go at recapping three different ways of formulating the law.

Functor Identity Law

The last two slides of this deck remind us of the **monad laws**.

They also make use of **Scala 3 extension methods**, this time to provide syntax for the infix operators for **flatMap** and **Kleisli composition**.

```
// MONAD LAWS
// left identity law: pure(a) flatMap f == f(a)assert( (pure(a) flatMap f) == f(a) )
// right identity law: ma flatMap pure == ma
assert( (f(a) flatMap pure) == f(a) )
assert( (a.some flatMap pure) == a.some )
assert( (none flatMap pure) == none )
// associativity law: ma flatMap f flatMap g = ma flatMap (a \Rightarrow f(a) flatMap g)assert( ((f(a) \text{ flatMap } g) \text{ flatMap } h) == (f(a) \text{ flatMap } (x \Rightarrow g(x) \text{ flatMap } h)) )assert( ((3.50me\text{ flatMap}\text{ g}) flatMap h) = (3.50me\text{ flatMap}\text{ (x = 3 g(x) flatMap}\text{ h}))assert( ((none flatMap g) flatMap h) == (none flatMap (x => g(x) flatMap h)) )
```

```
enum Option[+A]:
                                                               case Some(a: A)
                                                               case None
                                                               ... 
                                                             def flatMap[B](f: A => Option[B]): Option[B] =
                                                               this match
                                                                 case Some(a) \Rightarrow f(a)case None => None
                                                                ... 
                                                             object Option : 
                                                               def pure[A](a: A): Option[A] = Some(a)
                                                               def none: Option[Nothing] = None
                                                               def id[A](oa: Option[A]): Option[A] = oa
                                                             extension[A](a: A):
                                                               def some: Option[A] = Some(a)
                               val f = stringToInt
                               val g = intToChars
                               val h = charsToInt
                               val a = "123"
assert( stringToInt("123") == Some(123) )
assert( stringToInt("1x3") == None )
assert( intToChars(123) == Some(List('1', '2', '3'))) 
assert( intToChars(0) == Some(List('0'))) 
assert( intToChars(-10) == None)
assert(charsToInt(List('1', '2', '3')) == Some(123) )
assert(charsToInt(List('1', 'x', '3')) == None )
```


The **monad laws** again, but this time using a **Haskell**-style **bind** operator as an alias for **flatMap**.

```
// left identity law: pure(a) flatMap f = f(a)assert((pure(a) \geq f) = f(a))// right identity law: ma flatMap pure = ma
assert( (f(a) \approx pure) = f(a))
assert( (3.50me \n\equiv pure) = 3.50me)
assert( (none \succeq pure) = none)
// associativity law: ma flatMap f flatMap g = ma flatMap (a \Rightarrow f(a) flatMap g)
assert( ((f(a) \ge g) \ge h) = (f(a) \ge (x \Rightarrow g(x) \ge h)))assert( (3.50me \ge g) \ge h) = (3.50me \ge (x \Rightarrow g(x) \ge h)))assert( ((none \ge g) \ge h) = (none \ge ((x:Int) \Rightarrow g(x) \ge h)))
```


And here are the **monad laws** expressed in terms of **Kleisli composition** (the **fish operator**).

// left identity law: pure \implies f = f assert((pure[String] \implies f)(a) = f(a)) // right identity law: $f \implies pure = f$

$$
\overline{assert}(\ (f \Rightarrow pure)(a) = f(a)
$$

// associativity law :
$$
f \implies (g \implies h) = (f \implies g) \implies h
$$

assert(($f \implies (g \implies h))(a) = ((f \implies g) \implies h)(a)$)

 $extension[A,B](oa: Option[A])$ def \cong (f: A \Rightarrow Option[B]): Option[B] = oa flatMap f

extension[A,B,C](f: A \Rightarrow Option[B]) def \rightarrow (g: B \rightarrow Option[C]): A \rightarrow Option[C] = $a \Rightarrow f(a) \succcurlyeq g$

If you are new to functor laws and/or monad laws you might want to take a look at some of the following

https://www2.slideshare.net/pjschwarz/functor-laws

https://www2.slideshare.net/pjschwarz/monad-laws-must-be-checked-107011209

https://www2.slideshare.net/pjschwarz/rob-norrisfunctionalprogrammingwitheffects

That's all. I hope you found it useful.

@philip_schwarz