

From Subtype Polymorphism To Typeclass-based Ad hoc Polymorphism

An Example



slides by



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Here is a function that orders a list of integers using quicksort.

```
def order(ns: List[Int]): List[Int] = ns match
  case Nil => Nil
  case head :: tail =>
    val (smaller, larger) = tail.partition(_ < head)
    order(smaller) ++ List(head) ++ order(larger)

extension (ns: List[Int])
  def ordered: List[Int] = order(ns)
```

```
assert( List(4, 1, 3, 5, 2).ordered == List(1, 2, 3, 4, 5) )
```



What if we want to order people, e.g. by their age?

```
case class Person(name: String, age: Int)
```

Let's define a type to be **Orderable** if it provides a function for comparing its values so as to determine their relative order.

And now let's make **Person** an **Orderable**

```
case class Person(name: String, age: Int) extends Orderable[Person]:
  override def compare(other: Person): Int = this.age - other.age
```

```
assert( Person("John", 25) < Person("Jane", 30) )
```

```
trait Orderable[A]:
  def compare(other: A): Int

object Orderable:
  extension [A](l: Orderable[A])
    def <(r: A): Boolean = l.compare(r) < 0
```

Returns a negative integer, zero, or a positive integer as **this** is less than, equal to, or greater than **other**.

Getting **Person** to implement (mix-in) the **Orderable** trait.

Younger people come first



Now let's use **subtype polymorphism** and modify our **order** function so that rather than sorting a list of integers, it sorts a list of any type that is an **Orderable**.

[**A <: Orderable[A]**] means that the **order** function operates on lists whose element type **A** is a **subtype** of upper bound **Orderable**.

```
def order(ns: List[Int]): List[Int] = ns match
  case Nil => Nil
  case head :: tail =>
    val (smaller, larger) = tail.partition(_ < head)
    order(smaller) ++ List(head) ++ order(larger)

extension (ns: List[Int])
  def ordered: List[Int] = order(ns)
```

```
def order[A <: Orderable[A]](as: List[A]): List[A] = as match
  case Nil => Nil
  case head :: tail =>
    val (smaller, larger) = tail.partition(_ < head)
    order(smaller) ++ List(head) ++ order(larger)

extension [A <: Orderable[A]](as: List[A])
  def ordered: List[A] = order(as)
```

```
def order(ns: List[Int]): List[Int] = ns match
  case Nil => Nil
  case head :: tail =>
    val (smaller, larger) = tail.partition(_ < head)
    order(smaller) ++ List(head) ++ order(larger)
```

```
=> def order[A <: Orderable[A]](as: List[A]): List[A] = as match
  case Nil => Nil
  case head :: tail =>
    val (smaller, larger) = tail.partition(_ < head)
    order(smaller) ++ List(head) ++ order(larger)
```

```
extension (ns: List[Int])
  def ordered: List[Int] =
    order(ns)
```

```
=> extension [A <: Orderable[A]](as: List[A])
  def ordered: List[A] =
    order(as)
```



Let's sort some people.

```
val people = List( Person("Jane", 30), Person("John", 25), Person("Jim", 18) )
val peopleByIncreasingAge = List( Person("Jim", 18), Person("John", 25), Person("Jane", 30) )

assert(people.ordered == peopleByIncreasingAge)
```



Now we are able to sort people, but we are no longer able to sort integers, because `Int` does not implement (mix-in) the `Orderable` trait, and we cannot make it do so, because we don't own the `Int` type.

Enter **typeclasses**, which allow a more general solution that does not have this limitation.

Let's define a **typeclass** called `Order`, whose **instance** for type `A` provides a function for comparing `A` values so as to determine their relative order.

`(using order: Order[A])`
is a **context parameter**, often simply called a '**given**'.

```
trait Orderable[A]:  
  def compare(other: A): Int  
  
object Orderable:  
  extension [A](l: Orderable[A])  
    def <(r: A): Boolean = l.compare(r) < 0
```



```
trait Order[A]:  
  def compare(l: A, r: A): Int  
  
object Order:  
  extension [A](l: A)(using order: Order[A])  
    def <(r: A): Boolean = order.compare(l, r) < 0
```

| | | |
|--|----|---|
| trait Orderable[A]: def compare(other: A): Int | <> | trait Order[A]: def compare(l: A, r: A): Int |
| | = | |
| object Orderable: extension [A](l: Orderable[A]) def <(r: A): Boolean = l.compare(r) < 0 | <> | object Order: extension [A](l: A)(using order: Order[A]) def <(r: A): Boolean = order.compare(l, r) < 0 |



Now let's use **typeclass-based ad hoc polymorphism**, and modify our **order** function so that rather than ordering a list of any type that is **Orderable**, it sorts a list of any type for which there exists a 'given' instance of the **typeclass** called **Order**.

[**A: Order**] is a **context bound**, which is a shorthand syntax for (**using uvxyz: Order[A]**), so it means that function **order** has a **context parameter** of type **Order[A]**.

```
def order[A <: Orderable[A]](as: List[A]): List[A] = as match
  case Nil => Nil
  case head :: tail =>
    val (smaller, larger) = tail.partition(_ < head)
    order(smaller) ++ List(head) ++ order(larger)
```

```
extension [A<: Orderable[A]](as: List[A])
  def ordered: List[A] = order(as)
```

```
def order[A: Order](as: List[A]): List[A] = as match
  case Nil => Nil
  case head :: tail =>
    val (smaller, larger) = tail.partition(_ < head)
    order(smaller) ++ List(head) ++ order(larger)
```

```
extension [A: Order](as: List[A])
  def ordered: List[A] = order(as)
```

```
def order[A <: Orderable[A]](as: List[A]): List[A] = as match
  case Nil => Nil
  case head :: tail =>
    val (smaller, larger) = tail.partition(_ < head)
    order(smaller) ++ List(head) ++ order(larger)
```

```
extension [A <: Orderable[A]](as: List[A])
  def ordered: List[A] = order(as)
```

```
= def order[A: Order](as: List[A]): List[A] = as match
  case Nil => Nil
  case head :: tail =>
    val (smaller, larger) = tail.partition(_ < head)
    order(smaller) ++ List(head) ++ order(larger)
```

```
<> extension [A: Order](as: List[A])
  def ordered: List[A] = order(as)
```



To sort some integers we need to define a '**given**' instance of **Order** for **Int**.

```
given Order[Int] with  
  override def compare(l: Int, r: Int): Int = l - r
```

We decided not to give the **instance** a name. if we need to get hold of the **instance**, we can do so using the **summon** function

```
val order: Order[Int] = summon[Order[Int]]
```



To make **summoning** the **instance** more convenient, let's define the following **apply** function in the **Order** companion object

```
def apply[A](using orderable: Order[A]): Order[A] = orderable
```

```
val ascendingIntOrder: Order[Int] = Order[Int]
```

| | | |
|--|----|--|
| object Order: | = | object Order: |
| | <> | def apply[A](using orderable: Order[A]): Order[A] = orderable |
| extension [A](l: A)(using order: Order[A]) def <(r: A): Boolean = order.compare(l, r) < 0 | = | extension [A](l: A)(using order: Order[A]) def <(r: A): Boolean = order.compare(l, r) < 0 |



Let's sort some integers

```
val ints = List(4, 1, 3, 5, 2)  
val ascendingInts = List(1, 2, 3, 4, 5)
```

```
assert(ints.ordered == ascendingInts)
```

Our '**given**' instance of **typeclass Order[Int]** is **implicitly** passed as a parameter into the **ordered** and **order** functions.

```
assert(ints.ordered(using ascendingIntOrder) == ascendingInts)  
assert(ints.ordered(using Order[Int]) == ascendingInts)
```

If for some reason we want to pass the parameter **explicitly**, here are two ways we can do it.

```
assert(ints.ordered(using _ - _) == ascendingInts)
```

Interestingly, an **anonymous function** that subtracts its two parameters also qualifies as an **explicit Order[Int]** parameter (see next slide).

8.9 “SAM” types

... as in Java, Scala will allow a **function type** to be used where an **instance** of a **class** or **trait** declaring a **single abstract method (SAM)** is required. This will work with any **SAM**. For example, you might define a **trait**, **Increaser**, with a **single abstract method**, **increase**:

```
trait Increaser:  
  def increase(i: Int): Int
```

You could then define a method that takes an **Increaser**:

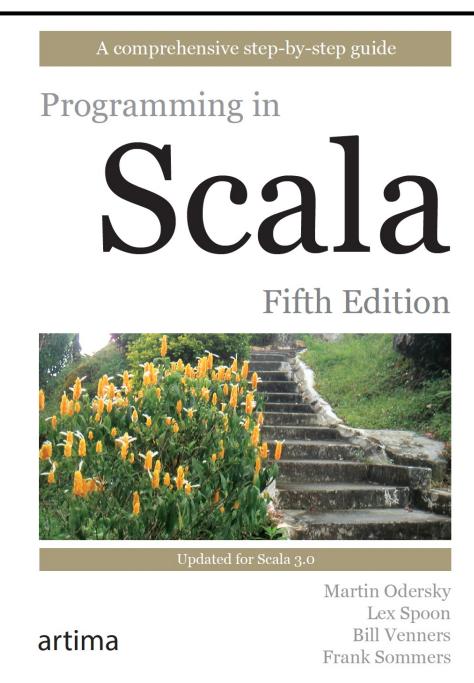
```
def increaseOne(increaser: Increaser): Int =  
  increaser.increase(1)
```

To invoke your new method, you could pass in an **anonymous instance** of **trait Increaser**, like this:

```
increaseOne(  
  new Increaser:  
    def increase(i: Int): Int = i + 7  
)
```

In Scala versions 2.12 and greater, however, you could alternatively just use a **function literal**, because **Increaser** is a **SAM type**:

```
increaseOne(i => i + 7) // Scala
```



```
assert(ints.ordered(using _ - _) == ascendingInts)
```

Because a **SAM** type is expected here, we can pass in a function literal, e.g. `_ - _`

```
trait Order[A]:  
  def compare(l: A, r: A): Int
```

Order is a **SAM** type (declares a **SAM**)

ordered, and **order** take an **implicit parameter** that is a **SAM** type

```
def order[A: Order](as: List[A]): List[A] = ...  
  
extension [A: Order](as: List[A])  
  def ordered: List[A] = order(as)
```



Now in the `Order` companion object, let's add a function that given an `Order` which orders elements in a certain way, returns a new `Order` that orders elements in the opposite way.

```
extension [A](order: Order[A])
def reverse: Order[A] = (l: A, r: A) => order.compare(r, l)
```

Note that we are comparing `r` with `l`, rather than the other way around.

| | | |
|---|----|--|
| object Order: | = | object Order: |
| def apply[A](using orderable: Order[A]): Order[A] = orderable | | def apply[A](using orderable: Order[A]): Order[A] = orderable |
| extension [A](l: A)(using order: Order[A]) def <(r: A): Boolean = order.compare(l, r) < 0 | <> | extension [A](l: A)(using order: Order[A]) def <(r: A): Boolean = order.compare(l, r) < 0 |
| | | extension [A](order: Order[A]) def reverse: Order[A] = (l: A, r: A) => order.compare(r, l) |



We can now order integers using the `reverse` of '`given`' `Order[Int]`, i.e. in descending order.

```
val descendingIntOrder = ascendingIntOrder.reverse

assert(ints.ordered(using descendingIntOrder) == ascendingInts.reverse)

assert(ints.ordered(using Order[Int].reverse) == ascendingInts.reverse)

assert(ints.ordered(using (n1, n2) => n2 - n1) == ascendingInts.reverse)
```



Let's do for **String** what we have done so far for **Int**.

To order **Strings** we define a '**given**' instance of **Order** for **String**.

```
given Order[String] with
  override def compare(l: String, r: String): Int = l.compareTo(r)
```

| | | |
|--|---|--|
| given Order[Int] with override def compare(l: Int, r: Int): Int = l - r | = | given Order[Int] with override def compare(l: Int, r: Int): Int = l - r |
|--|---|--|

| | | |
|--|-----|--|
| | --> | given Order[String] with override def compare(l: String, r: String): Int = l.compareTo(r) |
|--|-----|--|

```
val names = List("John", "Jane", "Jim")
val ascendingNames = List("Jane", "Jim", "John")

val ascendingStringOrder = Order[String]

assert(names.ordered == ascendingNames)
assert(names.ordered(using ascendingStringOrder) == ascendingNames)
assert(names.ordered(using Order[String]) == ascendingNames)
assert(names.ordered(using _ compareTo _) == ascendingNames)

val descendingStringOrder = ascendingStringOrder.reverse

assert(names.ordered(using descendingStringOrder) == ascendingNames.reverse)
assert(names.ordered(using Order[String].reverse) == ascendingNames.reverse)
assert(names.ordered(using (s1,s2) => s2 compareTo s1) == ascendingNames.reverse)
```



Now let's move on to ordering people.

We begin by undoing the changes that we made to **Person** in order to use **subtype polymorphism**, i.e. we stop **Person** from implementing (mixing-in) **Orderable**.

```
case class Person(name: String, age: Int) extends Orderable[Person]:  
  override def compare(other: Person): Int = this.age - other.age
```



```
case class Person(name: String, age: Int)
```

```
case class Person(name: String, age: Int) extends Orderable[Person]:  
  override def compare(other: Person): Int =  
    this.age - other.age
```



```
case class Person(name: String, age: Int)
```



With **Int**, it was natural for the '**given**' **Order[Int]** to be ascending order.
Similarly with **String**.

But what should be the default ordering for people? By ascending age?, By ascending name?
There isn't a natural order for people, so we are not going to provide a default.

Also, since age is an **Int** and name is a **String**, and since '**givens**' **Order[Int]** and **Order[String]** already exist, instead of defining an **Order[Person]** from scratch, we are going to define it in terms of one of those (see next slide).



If we have an `Order[B]` for ordering `Bs`, and we have a function that converts an `A` to a `B`, then we can easily create an `Order[A]` for ordering `As`.

```
extension [B](order: Order[B])
def on[A](f: A => B): Order[A] = (l: A, r: A) => order.compare(f(l), f(r))
```

| | | |
|--|----|---|
| object Order: | = | object Order: |
| def apply[A](using orderable: Order[A]): Order[A] = orderable | | def apply[A](using orderable: Order[A]): Order[A] = orderable |
| extension [A](l: A)(using order: Order[A]) def <(r: A): Boolean = order.compare(l, r) < 0 | | extension [A](l: A)(using order: Order[A]) def <(r: A): Boolean = order.compare(l, r) < 0 |
| extension [A](order: Order[A]) def reverse: Order[A] = (l: A, r: A) => order.compare(r, l) | -+ | extension [A](order: Order[A]) def reverse: Order[A] = (l: A, r: A) => order.compare(r, l) |
| | | extension [B](order: Order[B]) def on[A](f: A => B): Order[A] = (l: A, r: A) => order.compare(f(l), f(r)) |



Let's define some people.

```
val people = List(Person("Jane", 30), Person("John", 25), Person("Jim", 18))  
val peopleByAge = List(Person("Jim", 18), Person("John", 25), Person("Jane", 30))
```

Let's say that locally to a certain part of the application, we do want ordering by age to be the default.

```
given ageOrder: Order[Person] = ascendingIntOrder.on(_.age)
```

Create a `Person` order that is an ascending `Int` order `on` a person's age.

```
assert(Person("John", 25) < Person("Jane", 30))
```

Younger people come first



Now let's order the people by ascending age.

```
assert(people.ordered == peopleByAge)  
assert(people.ordered(using ageOrder) == peopleByAge)  
assert(people.ordered(using Order[Int].on[Person](_.age)) == peopleByAge)  
assert(people.ordered(using (p1, p2) => p1.age - p2.age) == peopleByAge)
```

And now by descending age

```
assert(people.ordered(using ageOrder.reverse) == peopleByAge.reverse)  
assert(people.ordered(using Order[Int].on[Person](_.age).reverse) == peopleByAge.reverse)  
assert(people.ordered(using (p1, p2) => p2.age - p1.age) == peopleByAge.reverse)
```



Same as on the previous slide, but here we are ordering people by name.

```
val people = List(Person("Jane", 30), Person("John", 25), Person("Jim", 18))  
val peopleByName = List(Person("Jane", 30), Person("Jim", 18), Person("John", 25))
```

```
val lexicographicStringOrder = Order[String]  
val nameOrder: Order[Person] = lexicographicStringOrder.on(_.name)
```

Create a `Person` order that is an ascending `String` order **on** a person's name.

First let's order the people by ascending name, and then by descending name.

```
assert(people.ordered == peopleByName)  
assert(people.ordered(using nameOrder) == peopleByName)  
assert(people.ordered(using Order[String].on[Person](_.name)) == peopleByName)  
assert(people.ordered(using (p1,p2) => p1.name - p2.name) == peopleByName)
```

```
assert(people.ordered(using nameOrder.reverse) == peopleByName.reverse)  
assert(people.ordered(using Order[String].on[Person](_.age).reverse) == peopleByName.reverse)  
assert(people.ordered(using (p1, p2) => p2.name - p1.name) == peopleByName.reverse)
```



To conclude the example, let's say that we want to order people first by age, and then by name, i.e. we want to order them by age, but when the age is the same, we want to order them by name.

Rather than defining a '**given**' ordering for this specific case, we are going to do the following:

1. define a generic '**given**' **Order**[(A, B)] for any A and B for which '**givens**' **Order**[A] and **Order**[B] exist.
2. define our desired **Order**[Person] applying our existing **on** function to **Order**[(Int, String)] (the latter exists because '**givens**' **Order**[Int] and **Order**[String] exist).

```
given [A, B](using oa: Order[A], ob: Order[B]): Order[(A, B)] with
  override def compare(l: (A, B), r: (A, B)): Int = (l, r) match
    case ((la, lb), (ra, rb)) =>
      val asComparison = oa.compare(la, ra)
      if asComparison == 0
        then ob.compare(lb, rb)
        else asComparison
```

| | | |
|--|----|--|
| given Order[Int] with override def compare(l: Int, r: Int): Int = l - r given Order[String] with override def compare(l: String, r: String): Int = l.compareTo(r) | = | given Order[Int] with override def compare(l: Int, r: Int): Int = l - r given Order[String] with override def compare(l: String, r: String): Int = l.compareTo(r) |
| | -+ | given [A, B](using oa: Order[A], ob: Order[B]): Order[(A, B)] with override def compare(l: (A, B), r: (A, B)): Int = (l, r) match case ((la, lb), (ra, rb)) => val asComparison = oa.compare(la, ra) if asComparison == 0 then ob.compare(lb, rb) else asComparison |



Now we can order people as desired.

```
val morePeople = List(Person("John", 25), Person("Jane", 30), Person("Jack", 25), Person("Jim", 18))
val morePeopleByAgeAndThenName = List(Person("Jim", 18), Person("Jack", 25), Person("John", 25), Person("Jane", 30))

val ageAndThenNameOrder: Order[Person] = Order[(Int, String)].on(p => (p.age, p.name))

assert(morePeople.ordered(using ageAndThenNameOrder) == morePeopleByAgeAndThenName)
```

Note that **John** and **Jack** are the same age.

Ordering integers

```
def order(ns: List[Int]): List[Int] = ns match
  case Nil => Nil
  case head :: tail =>
    val (smaller, larger) = tail.partition(_ < head)
    order(smaller) ++ List(head) ++ order(larger)

extension (ns: List[Int])
  def ordered: List[Int] = order(ns)
```

```
assert( List(4, 1, 3, 5, 2).ordered == List(1, 2, 3, 4, 5) )
```

Ordering people using **subtype polymorphism**

```
trait Orderable[A]:  
  def compare(other: A): Int  
  
object Orderable:  
  extension [A](l: Orderable[A])  
    def <(r: A): Boolean = l.compare(r) < 0
```

```
def order[A <: Orderable[A]](as: List[A]): List[A] = as match  
  case Nil => Nil  
  case head :: tail =>  
    val (smaller, larger) = tail.partition(_ < head)  
    order(smaller) ++ List(head) ++ order(larger)  
  
extension [A <: Orderable[A]](as: List[A])  
  def ordered: List[A] = order(as)
```

```
case class Person(name: String, age: Int) extends Orderable[Person]:  
  override def compare(other: Person): Int = this.age - other.age
```

```
val people = List( Person("Jane", 30), Person("John", 25), Person("Jim", 18) )  
val peopleByIncreasingAge = List( Person("Jim", 18), Person("John", 25), Person("Jane", 30) )  
  
assert(people.ordered == peopleByIncreasingAge)
```

Ordering integers, strings and people using typeclass-based ad hoc polymorphism

```
trait Order[A]:  
  def compare(l: A, r: A): Int  
  
object Order:  
  
  def apply[A](using orderable: Order[A]): Order[A] =  
    orderable  
  
  extension [A](l: A)(using order: Order[A])  
    def <(r: A): Boolean = order.compare(l, r) < 0  
  
  extension [A](order: Order[A])  
    def reverse: Order[A] = (l: A, r: A) =>  
      order.compare(r, l)  
  
  extension [B](order: Order[B])  
    def on[A](f: A => B): Order[A] = (l: A, r: A) =>  
      order.compare(f(l), f(r))
```

```
def order[A: Order](as: List[A]): List[A] = as match  
  case Nil => Nil  
  case head :: tail =>  
    val (smaller, larger) = tail.partition(_ < head)  
    order(smaller) ++ List(head) ++ order(larger)  
  
extension [A: Order](as: List[A])  
def ordered: List[A] = order(as)
```

```
given Order[Int] with  
  override def compare(l: Int, r: Int): Int = l - r  
  
given Order[String] with  
  override def compare(l: String, r: String): Int =  
    l.compareTo(r)  
  
given [A,B](using oa:Order[A], ob:Order[B]):Order[(A,B)] with  
  override def compare(l: (A, B), r: (A, B)): Int =  
    (l, r) match  
      case ((la, lb), (ra, rb)) =>  
        val asComparison = oa.compare(la, ra)  
        if asComparison == 0 then ob.compare(lb, rb)  
        else asComparison
```

```
case class Person(name: String, age: Int)
```

```
val order: Order[Int] = summon[Order[Int]]
```

```
val ascendingIntOrder: Order[Int] = Order[Int]
```

```
val ints = List(4, 1, 3, 5, 2)
val ascendingInts = List(1, 2, 3, 4, 5)
```

```
assert(ints.ordered == ascendingInts)
```

```
assert(ints.ordered(using ascendingIntOrder) == ascendingInts)
assert(ints.ordered(using Order[Int]) == ascendingInts)
```

```
assert(ints.ordered(using _ - _) == ascendingInts)
```

```
val descendingIntOrder = ascendingIntOrder.reverse
```

```
assert(ints.ordered(using descendingIntOrder) == ascendingInts.reverse)
assert(ints.ordered(using Order[Int].reverse) == ascendingInts.reverse)
assert(ints.ordered(using (n1, n2) => n2 - n1) == ascendingInts.reverse)
```

```
val names = List("John", "Jane", "Jim")
val ascendingNames = List("Jane", "Jim", "John")

val ascendingStringOrder = Order[String]

assert(names.ordered == ascendingNames)
assert(names.ordered(using ascendingStringOrder) == ascendingNames)
assert(names.ordered(using Order[String]) == ascendingNames)
assert(names.ordered(using _ compareTo _) == ascendingNames)

val descendingStringOrder = ascendingStringOrder.reverse

assert(names.ordered(using descendingStringOrder) == ascendingNames.reverse)
assert(names.ordered(using Order[String].reverse) == ascendingNames.reverse)
assert(names.ordered(using (s1,s2) => s2 compareTo s1) == ascendingNames.reverse)
```

```
val people = List(Person("Jane", 30), Person("John", 25), Person("Jim", 18))
val peopleByAge = List(Person("Jim", 18), Person("John", 25), Person("Jane", 30))
```

```
given ageOrder: Order[Person] = ascendingIntOrder.on(_.age)
```

```
assert(Person("John", 25) < Person("Jane", 30))
```

```
assert(people.ordered == peopleByAge)
assert(people.ordered(using ageOrder) == peopleByAge)
assert(people.ordered(using Order[Int].on[Person](_.age)) == peopleByAge)
assert(people.ordered(using (p1, p2) => p1.age - p2.age) == peopleByAge)
```

```
assert(people.ordered(using ageOrder.reverse) == peopleByAge.reverse)
assert(people.ordered(using Order[Int].on[Person](_.age).reverse) == peopleByAge.reverse)
assert(people.ordered(using (p1, p2) => p2.age - p1.age) == peopleByAge.reverse)
```

```
val people = List(Person("Jane", 30), Person("John", 25), Person("Jim", 18))
val peopleByName = List(Person("Jane", 30), Person("Jim", 18), Person("John", 25))
```

```
val lexicographicStringOrder = Order[String]
val nameOrder: Order[Person] = lexicographicStringOrder.on(_.name)
```

```
assert(people.ordered == peopleByName)
assert(people.ordered(using nameOrder) == peopleByName)
assert(people.ordered(using Order[String].on[Person](_.name)) == peopleByName)
assert(people.ordered(using (p1,p2) => p1.name - p2.name) == peopleByName)
```

```
assert(people.ordered(using nameOrder.reverse) == peopleByName.reverse)
assert(people.ordered(using Order[String].on[Person](_.age).reverse) == peopleByName.reverse)
assert(people.ordered(using (p1, p2) => p2.name - p1.name) == peopleByName.reverse)
```

```
val morePeople = List(Person("John", 25), Person("Jane", 30), Person("Jack", 25), Person("Jim", 18))
val morePeopleByAgeAndThenName = List(Person("Jim", 18), Person("Jack", 25), Person("John", 25), Person("Jane", 30))

val ageAndThenNameOrder: Order[Person] = Order[(Int, String)].on(p => (p.age, p.name))

assert(morePeople.ordered(using ageAndThenNameOrder) == morePeopleByAgeAndThenName)
```



That's all – I hope you found it useful



inspired
by

Ad hoc Polymorphism using Type Classes

wholly based on 'How to write like Cats', a great talk by Monty West



Monty West
<https://www.linkedin.com/in/monty-west/>



YouTube How to write like Cats by Monty West <https://github.com/MontyWest/tech-talk-typeclass>



<https://fpilluminated.com/>

slides by   @philip_schwarz
 <https://www.slideshare.net/pjschwarz>

