Fusing Transformations of Strict Scala Collections with Views

learn about it through the work of...



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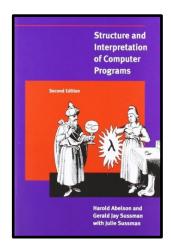
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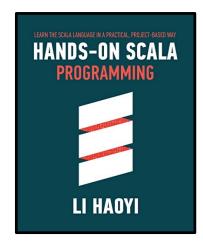
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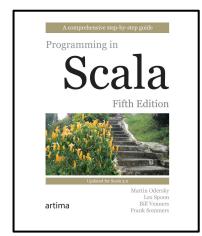


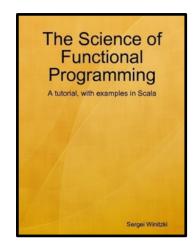
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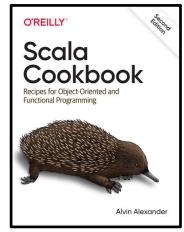
















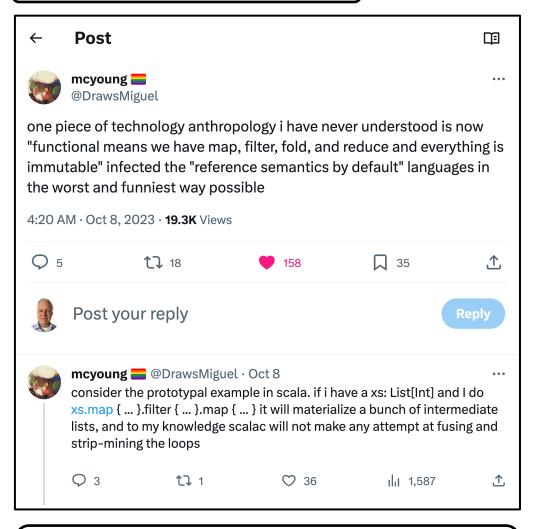






@philip_schwarz

This deck was inspired by the following tweet.



With excerpts from some great books, this deck aims to provide a good introduction to how the **transformations** of **eager collections**, e.g. **map** and **filter**, can be **fused** using **views**.





There is a lot of overlap between the subject of **views**, and that of **streams**. For example, they both address the problem of **fusing transformations**, and they both do it using **laziness**.

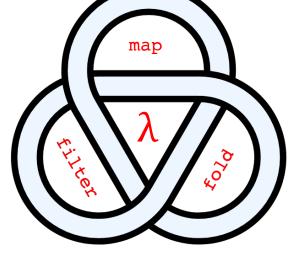
Because of that, I think it can be useful, before diving into the subject of **views**, to first go through a brief refresher on (or introduction to) **streams**.

If you prefer to go straight to the main subject of the deck then you can just jump to slide 13.

Among the many **transformer methods** of collections (methods that create new collections), **map** and **filter** stand out as members of the following triad that is the bread, butter and jam of functional programming.











```
def product_of_squares_of_odd_elements(sequence: List[Int]): Int =
    sequence.filter(isOdd)
        .map(square)
        .foldRight(1)(_*_)
```



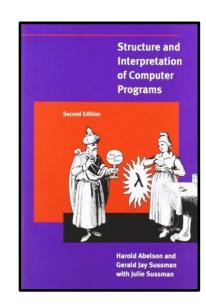




I first came across the map, filter and fold triad many years ago, at university, while reading Structure and Interpretation of Computer Programs (SICP).

The following four slides consist of **SICP** excerpts introducing the following two ideas:

- Transformations of strict/eager lists are severely inefficient, because they require creation and copying of data structures (that may be huge) at every step of a process (sequence of transformations).
- 2) Streams are a clever idea that exploits delayed evaluation (non-strictness/laziness) to permit the use of transformations without incurring some of the costs of manipulating strict/eager lists.



3.5 Streams

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From an abstract point of view, a stream is simply a sequence.

However, we will find that the straightforward implementation of streams as lists (as in section 2.2.1) doesn't fully reveal the power of stream processing.

2.2.1 Representing Sequences

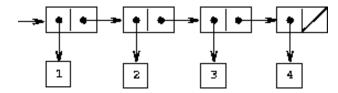


Figure 2.4: The sequence 1,2,3,4 represented as a chain of pairs.

One of the useful structures we can build with pairs is a <u>sequence</u> -- <u>an ordered collection of data objects</u>. There are, of course, many ways to represent <u>sequences</u> in terms of <u>pairs</u>. One particularly straightforward representation is illustrated in figure 2.4, where <u>the sequence</u> 1, 2, 3, 4 is represented as a <u>chain of pairs</u>. The <u>car</u> of each <u>pair</u> is the corresponding item in the <u>chain</u>, and the <u>cdr</u> of the pair is the next <u>pair</u> in the <u>chain</u>. The <u>cdr</u> of the final <u>pair</u> signals the end of the <u>sequence</u> by pointing to a <u>distinguished value</u> that is not a <u>pair</u>, represented in box-and-pointer diagrams as a diagonal line and in programs as the value of the variable <u>nil</u>. The entire sequence is <u>constructed by nested cons operations</u>:

As an alternative, we introduce the technique of *delayed evaluation*, which enables us to represent very large (even infinite) sequences as streams. Stream processing lets us model systems that have state without ever using assignment or mutable data.



Structure and Interpretation of Computer Programs

3.5.1 Streams Are Delayed Lists

As we saw in section 2.2.3, sequences can serve as standard interfaces for combining program modules. We formulated powerful abstractions for manipulating sequences, such as <u>map</u>, <u>filter</u>, and <u>accumulate</u>, that capture a wide variety of operations in a manner that is both succinct and elegant.

```
map:: (\alpha \rightarrow \beta) \rightarrow [\alpha] \rightarrow [\beta]map f[]= []map f(x:xs)= fx:mapfxs
```

```
filter:: (\alpha \rightarrow Bool) \rightarrow [\alpha] \rightarrow [\alpha]filter p []= []filter p (x:xs)= if pxthen x: filter p xselse filter p xs
```

```
\begin{array}{ll}
foldr & :: (\alpha \to \beta \to \beta) \to \beta \to [\alpha] \to \beta \\
foldr f e [] & = e \\
foldr f e (x:xs) & = f x (foldr f e xs)
\end{array}
```

<u>Unfortunately, if we represent sequences as lists, this elegance is bought at the price of severe inefficiency with respect to both the time and space required by our computations. When we represent manipulations on sequences as transformations of lists, our programs must construct and copy data structures (which may be huge) at every step of a process.</u>



Structure and Interpretation of Computer Programs

To see why this is true, let us compare two programs for computing the sum of all the prime numbers in an interval. The first program is written in standard <u>iterative style</u>:53

The second program performs the same computation using the sequence operations of section 2.2.3:

In carrying out the computation, the first program needs to store only the sum being accumulated. In contrast, the filter in the second program cannot do any testing until enumerate-interval has constructed a complete list of the numbers in the interval.

The <u>filter generates</u> <u>another list</u>, <u>which in turn is passed to accumulate</u> <u>before being collapsed to form a sum.</u>

Such large intermediate storage is not needed by the first program, which we can think of as enumerating the interval incrementally, adding each prime to the sum as it is generated.

⁵³ Assume that we have a predicate **prime?** (e.g., as in section <u>1.2.6</u>) that tests for **primality**.



Structure and Interpretation of Computer Programs

The <u>inefficiency</u> in using <u>lists</u> <u>becomes</u> <u>painfully apparent</u> if we use the <u>sequence</u> paradigm to compute the second prime in the interval from 10,000 to 1,000,000 by evaluating the expression

This expression does find the second prime, but the computational overhead is outrageous. We construct a list of almost a million integers, filter this list by testing each element for primality, and then ignore almost all of the result.

In a more traditional programming style, we would interleave the enumeration and the filtering, and stop when we reached the second prime.

Streams are a clever idea that allows one to use sequence manipulations without incurring the costs of manipulating sequences as lists.

With streams we can achieve the best of both worlds: We can formulate programs elegantly as sequence manipulations, while attaining the efficiency of incremental computation.

The basic idea is to arrange to construct a stream only partially, and to pass the partial construction to the program that consumes the stream.

If the consumer attempts to access a part of the stream that has not yet been constructed, the stream will automatically construct just enough more of itself to produce the required part, thus preserving the illusion that the entire stream exists.

In other words, although we will write programs as if we were processing complete sequences, we design our stream implementation to automatically and transparently interleave the construction of the stream with its use.



Structure and Interpretation of Computer Programs



Chapter 5 of Functional Programming in Scala explains how lazy lists (streams) can be used to fuse together sequences of transformations.

See the next slide for how the book introduces the problem that **streams** are meant to solve.

Chapter 5 - Strictness and laziness

In chapter 3 we talked about purely functional data structures, using singly linked lists as an example. We covered a number of bulk operations on lists—map, filter, foldLeft, foldRight, zipWith, and so on. We noted that each of these operations makes its own pass over the input and constructs a fresh list for the output.

Imagine if you had a deck of cards and you were asked to remove the odd-numbered cards and then flip over all the queens. Ideally, you'd make a single pass through the deck, looking for queens and odd-numbered cards at the same time. This is more efficient than removing the odd cards and then looking for queens in the remainder. And yet the latter is what Scala is doing in the following code:

```
scala> List(1,2,3,4).map(_ + 10).filter(_ % 2 == 0).map(_ * 3)
List(36,42)
```

In this expression, map(_ + 10) will produce an intermediate list that then gets passed to filter(_ % 2 == 0), which in turn constructs a list that gets passed to map(_ * 3), which then produces the final list. In other words, each transformation will produce a temporary list that only ever gets used as input to the next transformation and is then immediately discarded.

• • •

This view makes it clear how the calls to map and filter each perform their own traversal of the input and allocate lists for the output. Wouldn't it be nice if we could somehow fuse sequences of transformations like this into a single pass and avoid creating temporary data structures?

We could rewrite the code into a while loop by hand, but ideally we'd like to have this done automatically while retaining the same highlevel compositional style. We want to compose our programs using higher-order functions like **map** and **filter** instead of writing monolithic loops.

It turns out that we can accomplish this kind of automatic loop fusion through the use of non-strictness (or, less formally, laziness). In this chapter, we'll explain what exactly this means, and we'll work through the implementation of a lazy list type that fuses sequences of transformations. Although building a "better" list is the motivation for this chapter, we'll see that non-strictness is a fundamental technique for improving on the efficiency and modularity of functional programs in general.

• • •

5.2 An extended example: lazy lists

Let's now return to the problem posed at the beginning of this chapter. We'll explore how laziness can be used to improve the efficiency and modularity of functional programs using lazy lists, or streams, as an example. We'll see how chains of transformations on streams are fused into a single pass through the use of laziness. Here's a simple Stream definition...



Runar Bjarnason





Functional Programming

In Scala

Paul Chiusano

@pchiusano



Michael Pilquist



With that refresher on (or introduction to) **streams** out of the way, let's get back to the actual subject of this deck: **views**.

In my view (pun not intended) a great book to get started with is **Li Haoyi**'s **Hands-On Scala Programming**. I find its approach to introducing **views** unique, and I love how he includes diagrams to illustrate the concept.

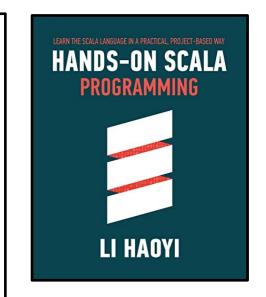
```
4.1.3 Transforms
@ Array(1, 2, 3, 4, 5).map(i \Rightarrow i * 2) // Multiply every element by 2
res7: Array[Int] = Array(2, 4, 6, 8, 10)
@ Array(1, 2, 3, 4, 5). filter(i \Rightarrow i \% 2 == 1) // Keep only elements not divisible by 2
res8: Array[Int] = Array(1, 3, 5)
@ Array(1, 2, 3, 4, 5).take(2) // Keep first two elements
res9: Array[Int] = Array(1, 2)
@ Array(1, 2, 3, 4, 5).drop(2) // Discard first two elements
res10: Array[Int] = Array(3, 4, 5)
@ Array(1, 2, 3, 4, 5).slice(1, 4) // Keep elements from index 1-4
res11: Array[Int] = Array(2, 3, 4)
@ Array(1, 2, 3, 4, 5, 4, 3, 2, 1, 2, 3, 4, 5, 6, 7, 8).distinct // Removes all duplicates
```

res15: Int = 1

res16: Int = 11

@ a2(0)

```
res12: Array[Int] = Array(1, 2, 3, 4, 5, 6, 7, 8)
Transforms take an existing collection and create a new
collection modified in some way. Note that these
transformations create copies of the collection, and leave the
original unchanged. That means if you are still using the original
array, its contents will not be modified by the transform.
@ val a2 = a.map(x => x + 10)
a2: Array[Int] = Array(11, 12, 13, 14, 15)
@ a(0) // Note that `a` is unchanged!
```



Li Haoyi

@lihaoyi



The copying involved in these collection transformations does have some overhead, but in most cases that should not cause issues. If a piece of code does turn out to be a bottleneck that is slowing down your program, you can always convert your .map/.filter/etc. transformation code into mutating operations over raw Arrays or In-Place Operations (4.3.4) over Mutable Collections (4.3) to optimize for performance.

4.1.6 Combining Operations

It is common to chain more than one operation together to achieve what you want. For example, here is a function that computes the standard deviation of an array of numbers:

```
@ def stdDev(a: Array[Double]): Double = {
  val mean = a.foldLeft(0.0)(_ + _) / a.length
  val squareErrors = a.map(_ - mean).map(x => x * x)
  math.sqrt(squareErrors.foldLeft(0.0)(_ + _) / a.length)
}
```

Scala collections provide a convenient helper method .sum that is equivalent to $.foldLeft(0.0)(_+_)$, so the above code can be simplified to...

As another example, here is a function that...

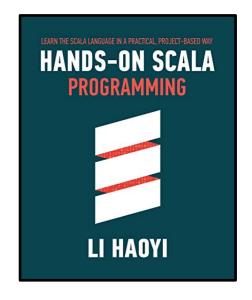
<u>Chaining collection transformations in this manner will always have some overhead</u>, <u>but for most use cases the overhead is worth the convenience and simplicity that these transforms give you</u>. If collection transforms do become a bottleneck, you can optimize the code using Views (4.1.8), In-Place Operations (4.3.4), or finally by looping over the raw Arrays yourself.

4.1.8 Views

When you chain multiple transformations on a collection, we are creating many intermediate collections that are immediately thrown away. For example, in the following snippet:

```
@ val myArray = Array(1, 2, 3, 4, 5, 6, 7, 8, 9)
@ val myNewArray = myArray.map(x => x + 1).filter(x => x % 2 == 0).slice(1, 3)
myNewArray: Array[Int] = Array(4, 6)
```

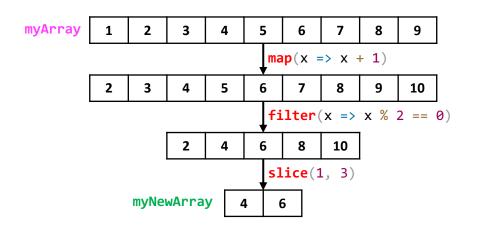
The chain of .map .filter .slice operations ends up traversing the collection three times, creating three new collections, but only the last collection ends up being stored in myNewArray and the others are discarded.



Li Haoyi

@lihaoyi

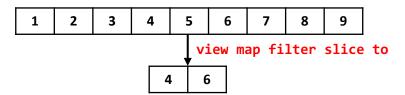




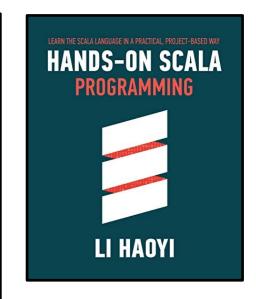
This creation and traversal of intermediate collections is wasteful. In cases where you have long chains of collection transformations that are becoming a performance bottleneck, you can use the .view method together with .to to "fuse" the operations together:

```
@ val myNewArray = myArray.view.map(_ + 1).filter(_ % 2 == 0).slice(1, 3).to(Array)
myNewArray: Array[Int] = Array(4, 6)
```

<u>Using .view before the map/filter/slice transformation operations defers the actual traversal and creation of a new collection until later, when we call .to to convert it back into a concrete collection type:</u>



This allows us to perform this chain of map/filter/slice transformations with only a single traversal, and only creating a single output collection. This reduces the amount of unnecessary processing and memory allocations.



Li Haoyi

@lihaoyi

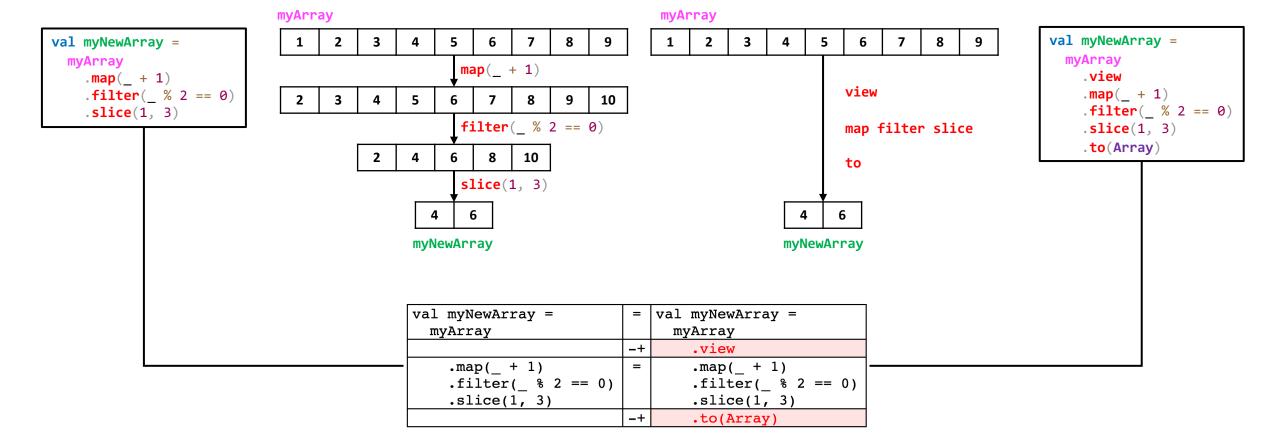




The next slide is just a quick visual recap.

- 3 traversals
- 3 collections created (2 intermediate ones)

- 1 traversal
- 1 collection created (no intermediate ones)
- call to view fuses map filter and slice together
- traversal is deferred until conversion to a concrete collection using .to





Next, let's turn to 'The' Scala book.

24.13 Views

Collections have quite a few methods that construct new collections. Some examples are map, filter, and ++.

We call such methods transformers because they take at least one collection as their receiver object and produce another collection in their result.

<u>Transformers</u> can be implemented in two principal ways: strict and nonstrict (or lazy).

A strict transformer constructs a new collection with all of its elements.

A non-strict, or lazy, transformer constructs only a proxy for the result collection, and its elements are constructed on demand.

As an example of a non-strict transformer, consider the following implementation of a lazy map operation:

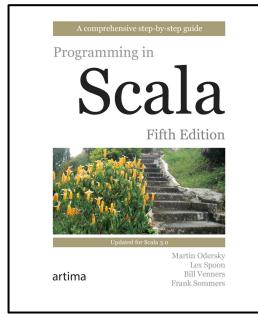
```
def lazyMap[T, U](col: Iterable[T], f: T => U) =
  new Iterable[U]:
    def iterator = col.iterator.map(f)
```

Note that lazyMap constructs a new Iterable without stepping through all elements of the given collection coll. The given function f is instead applied to the elements of the new collection's iterator as they are demanded.

Scala collections are by default strict in all their transformers, except for LazyList, which implements all its transformer methods lazily.

However, there is a systematic way to turn every collection into a lazy one and vice versa, which is based on collection views. A view is a special kind of collection that represents some base collection, but implements all of its transformers lazily.

To go from a collection to its view, you can use the view method on the collection. If xs is some collection, then xs.view is the same collection, but with all transformers implemented lazily. To get back from a view to a strict collection, you can use the to conversion operation with a strict collection factory as parameter.





Martin Odersky

@odersky

As an example, say you have a vector of Ints over which you want to map two functions in succession:

```
val v = Vector((1 to 10)*)
// Vector(1, 2, 3, 4, 5, 6, 7, 8, 9, 10)
v.map(_ + 1).map(_ * 2)
// Vector(4, 6, 8, 10, 12, 14, 16, 18, 20, 22)
```

In the last statement, the expression $v.map(_+ 1)$ constructs a new vector that is then transformed into a third vector by the second call to $map(_+ 2)$.

In many situations, constructing the intermediate result from the first call to map is a bit wasteful. In the pseudo example, it would be faster to do a single map with the composition of the two functions (_ + 1) and (_ * 2).

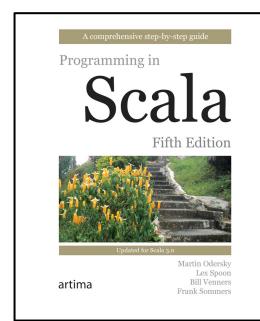
If you have the two functions available in the same place you can do this by hand. <u>But quite often, successive transformations</u> of a data structure are done in different program modules. <u>Fusing those transformations would then undermine modularity</u>. A more general way to avoid the <u>intermediate results</u> is by turning the vector first into a view, applying all <u>transformations</u> to the view, and finally forcing the view to a vector:

```
(v.view.map(_ + 1).map(_ * 2)).toVector
// Vector(4, 6, 8, 10, 12, 14, 16, 18, 20, 22)
```

We'll do this sequence of operations again, one by one:

```
scala> val vv = v.view
val vv: scala.collection.IndexedSeqView[Int] = IndexedSeqView(<not computed>)
```

The application v.view gives you an IndexedSeqView, a lazily evaluated IndexedSeq. As with LazyList, toString on views does not force the view elements. That's why the vv's elements are displayed as not computed.





Bill Venners

@bvenners

Applying the first map to the view gives you:

```
scala> vv.map(_ + 1)
val res13: scala.collection.IndexedSeqView[Int] = IndexedSeqView(<not computed>)
```

The result of the map is another IndexedSeqView[Int] value. This is in essence a <u>wrapper</u> that records the fact that a <u>map</u> with function $(_+ 1)$ needs to be applied on the vector \underline{v} . It does not apply that <u>map</u> until the <u>view</u> is forced, however.

We'll now apply the second map to the last result.

```
scala> res13.map(_ * 2)
val res14: scala.collection.IndexedSeqView[Int] = IndexedSeqView(<not computed>)
```

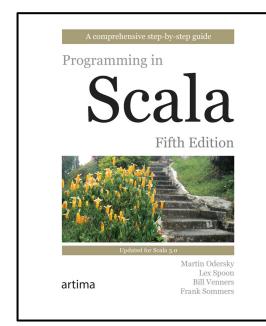
Finally, forcing the last result gives:

```
scala> res14.toVector
val res15: Seq[Int] = Vector(4, 6, 8, 10, 12, 14, 16, 18, 20, 22)
```

Both stored functions, (_ + 1) and (_ * 2), get applied as part of the execution of the to operation and a new vector is constructed. That way, no intermediate data structure is needed.

<u>Transformation</u> operations applied to <u>views</u> don't build a <u>new data structure</u>. <u>Instead, they return an iterable whose iterator is the result of applying the transformation operation to the underlying collection's iterator.</u>

<u>The main reason for using views is performance</u>. You have seen that by switching a collection to a view the construction of intermediate results can be avoided. These savings can be guite important.





Lex Spoon

As another example, consider the problem of finding the first palindrome in a list of words. A palindrome is a word that reads backwards the same as forwards. Here are the necessary definitions:

```
def isPalindrome(x: String) = x == x.reverse

def findPalindrome(s: Iterable[String]) = s.find(isPalindrome)
```

Now, assume you have a very long sequence, words, and you want to find a palindrome in the first million words of that sequence. Can you re-use the definition of findPalindrome? Of course, you could write:

```
findPalindrome(words.take(1000000))
```

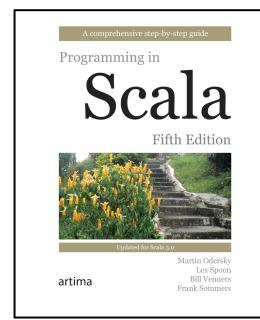
This nicely separates the two aspects of taking the first million words of a sequence and finding a palindrome in it. But the downside is that it always constructs an intermediary sequence consisting of one million words, even if the first word of that sequence is already a palindrome. So potentially, 999,999 words are copied into the intermediary result without being inspected at all afterwards. Many programmers would give up here and write their own specialized version of finding palindromes in some given prefix of an argument sequence. But with views, you don't have to.

Simply write:

```
findPalindrome(words.view.take(1000000))
```

This has the same nice separation of concerns, but <u>instead of a sequence of a million elements</u> it will only <u>construct</u> a single lightweight view object. This way, you do not need to choose between <u>performance</u> and <u>modularity</u>.

After having seen all these nifty uses of views you might wonder why have strict collections at all? One reason is that performance comparisons do not always favor lazy over strict collections. For smaller collection sizes the added overhead of forming and applying closures in views is often greater than the gain from avoiding the intermediary data structures. A possibly more important reason is that evaluation in views can be very confusing if the delayed operations have side effects.





Frank Sommers



In the next excerpt, **Sergei Winitzki**'s coverage of views, in the **Science of Functional Programming**, is short and sweet, but also nice and practical, with an emphasis on memory usage.

The code (1L to 1_000_000_000L).sum works because (1 to n) produces a sequence whose elements are computed whenever needed but do not remain in memory. This can be seen as a sequence with the "on-call" availability of elements. Sequences of this sort are called iterators:

```
scala> 1 to 5
res0: scala.collection.immutable.Range.Inclusive = Range(1, 2, 3, 4, 5)
scala> 1 until 5
res1: scala.collection.immutable.Range = Range(1, 2, 3, 4)
```

<u>The types Range and Range.Inclusive</u> are defined in the Scala standard library and are iterators. They behave as collections and support the usual methods (map, filter, etc.), but <u>they do not store previously computed values in memory</u>.

The view method

<u>Eager collections such as List or Array can be converted to iterators by using the view method.</u> This is necessary when intermediate collections consume too much memory when fully evaluated.

For example, consider the computation of Example 2.1.5.7 where we used flatMap to replace each element of an initial sequence by three new numbers before computing max of the resulting collection. If instead of three new numbers we wanted to compute three million new numbers each time, the intermediate collection created by flatMap would require too much memory, and the computation would crash:

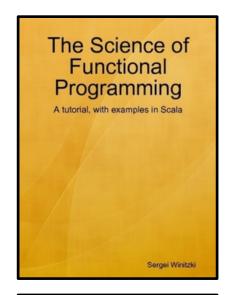
```
scala> (1 to 10).flatMap(x => 1 to 3_000_000).max
java.lang.OutOfMemoryError: GC overhead limit exceeded
```

NOTES (from 'Programming in Scala'): In Scala versions before 2.8, the **Range** type was **lazy**, so it behaved in effect like a **view**. Since 2.8, all collections except **lazy lists** and **views** are **strict**. The only way to go from a **strict** to a **lazy** collection is via the **view** method. The only way to go back is via **to**.

Even though the range (1 to 10) is an iterator, a subsequent flatMap operation creates an intermediate collection that is too large for our computer's memory.

We can use view to avoid this:

```
scala> (1 to 10).view.flatMap(x => 1 to 3_000_000).max
res0: Int = 3_000_000
```





Sergei Winitzki
in sergei-winitzki-11a6431



And last, but not by no means least, let's look at Alvin Alexander's Scala Cookbook recipe for Creating a Lazy View on a Collection.

11.4 Creating a Lazy View on a Collection

Problem

You're working with a large collection and want to create a lazy version of it so it will only compute and return results as they are needed.

Solution

Create a view on the collection by calling its view method. That creates a new collection whose transformer methods are implemented in a nonstrict, or lazy, manner. For example, given a large list:

```
val xs = List.range(0, 3_000_000) // a list from 0 to 2,999,999
```

imagine that you want to call several transformation methods on it, such as map and filter. This is a contrived example, but it demonstrates a problem:

```
val ys = xs.map(_ + 1).map(_ * 10).filter(_ > 1_000).filter(_ < 10_000)</pre>
```

If you attempt to run that example in the REPL, you'll probably see this fatal "out of memory" error:

```
scala> val ys = xs.map(_ + 1) java.lang.OutOfMemoryError: GC overhead limit exceeded
```

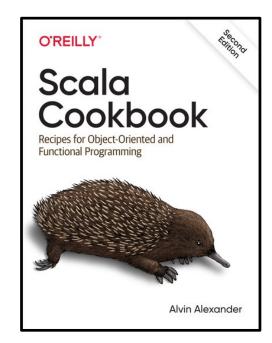
Conversely, this example returns almost immediately and doesn't throw an error because all it does is create a view and then four lazy transformer methods:

```
val ys = xs.view.map(_ + 1).map(_ * 10).filter(_ > 1_000).filter(_ < 10_000)
// result: ys: scala.collection.View[Int] = View(<not computed>)
```

Now you can work with ys without running out of memory:

```
scala> ys.take(3).foreach(println)
1010
1020
1030
```

<u>Calling view on a collection makes the resulting collection lazy.</u> Now when <u>transformer methods</u> are called on the <u>view</u>, <u>the</u> elements will only be calculated as they are accessed, and not "eagerly," as they normally would be with a strict collection.





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Discussion

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The use case for views

The main use case for using a view is performance, in terms of speed, memory, or both.

Regarding performance, the example in the Solution first demonstrates (a) a strict approach that runs out of memory, and then (b) a lazy approach that lets you work with the same dataset.

The problem with the first solution is that <u>it attempts to create new</u>, <u>intermediate collections</u> <u>each time a</u> <u>transformer method</u> <u>is called</u>:

If the initial collection a has one billion elements, the first map call creates a new intermediate collection with another billion elements.

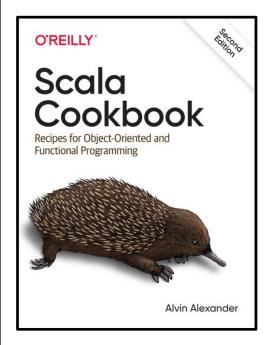
The second map call creates another collection, so now we're attempting to hold three billion elements in memory, and so on.

To drive that point home, that approach is the same as if you had written this:

Conversely, when you immediately create a view on the collection, everything after that essentially just creates an iterator:

```
val ys = a.view.map ... // this DOES NOT create another one billion elements
```

As usual with anything related to performance, be sure to test using a view versus not using a view in your application to find what works best. Another performance-related reason to understand views is that it's become very common to work with large datasets in a streaming manner, and views work very similar to streams.





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That's all. I hope you found it useful.